**Applecross Senior High School**

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**Western Australian Certificate of Education**

**Semester One Examination, 2015**

**Question/Answer Booklet**

**MATHEMATICS:**

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98

**SPECIALIST**

**UNIT 1**

**Section Two:**

**Calculator- assumed Score for this booklet**

**Student’s Name**: **\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_**

**As shown on your exam timetable.**

**Student’s Teacher Mr Bellis Mrs Waddell**

(**Circle your teacher’s name**.)

**Time allowed for this section**

Reading time before commencing work: ten minutes

Working time for this section: one hundred minutes

**Materials required/recommended for this section**

***To be provided by the supervisor***

This question /Answer Booklet

Formula Sheet (retained from Section One)

***To be provided by the candidate***

Standard Items: pens (blue/black preferred), pencils (including coloured), sharpener,

correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper,

and up to three calculators approved for use in the WACE examinations

**Important note to candidates**

No other items may be taken into the examination room. It is **your** responsibility to ensure

that you do not have any unauthorized notes or other items of a non-personal nature in the

examination room. If you have any unauthorized material with you, hand it to the supervisor

**before** reading any further.

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| Section | Number of questions available | Number of questions to be answered | Working time (minutes) | | Marks available | Percentage of exam |
| Section One:  Calculator-free | 7 | 7 | 50 | | 52 | 35 |
| Section Two:  Calculator-assumed | 13 | 13 | 100 | | 98 | 65 |
|  | | | | **Total** | 150 | 100 |

## Instructions to candidates

1. The rules for the conduct of examinations are detailed in the *School Examination Rules* provided with your exam timetable.Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer Booklet.
3. You must be careful to confine your responses to the specific questions asked and to follow any instructions that are specific to a particular question.
4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

* Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
* Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question(s) that you are continuing to answer at the top of the page.

1. **Show all your working clearly**. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
2. It is recommended that you **do not use pencil**, except in diagrams.
3. The formula sheet and your notes are **not to be handed** in with your Question/Answer Booklet.

Section Two: Calculator-assumed (98 Marks)

This section has**thirteen (****13)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time for this section is 100 minutes.

**Question 8 (5 marks)**

Three vectors are given by ,  and .

(a) Use your calculator to determine the angle between , to the nearest degree.

(2 marks)

(b) Determine all possible values of  if  and  are perpendicular. (3 marks)

**Question 9 (8 marks)**

(a) A multiple choice test has twelve questions and each question has three possible choices. If all questions are attempted, in how many ways can the test be answered? (2 marks)

(b) A set S contains all the integers between 3 and 102 inclusive. Determine

(i) how many numbers in set S are multiples of 7. (1 mark)

(ii) how many numbers in set S are multiples of 3 or 7. (2 marks)

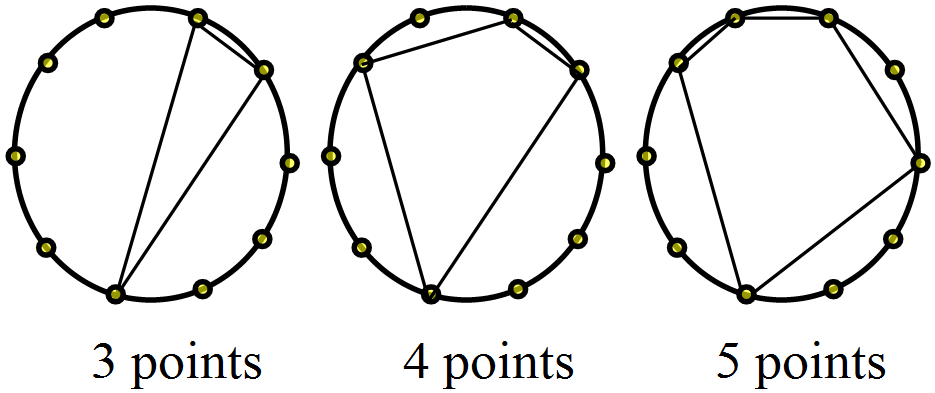
(iii) how many numbers in set S are multiples of either 3 or 7 but not both. (1 mark)

(c) Ten points are equally spaced around the circumference of a circle.

Determine the number of simple (non-self-intersecting) convex polygons that can

be formed by joining either three, four or five of these points with straight line segments

(as in the examples below). (2 marks)



**Question 10 (7 marks)**

Three forces are applied to a body. One has magnitude 300 N and acts due south. Another has magnitude 250 N and acts on a bearing of 050º.

(a) If the third force has a magnitude of 350 N and acts on a bearing of 250º, determine the magnitude and direction of the resultant force. (6 marks)

(b) A 4th force is applied so that the body is in equilibrium. Use your answer from part a) to write down the magnitude and direction of the 4th force. (1 mark)

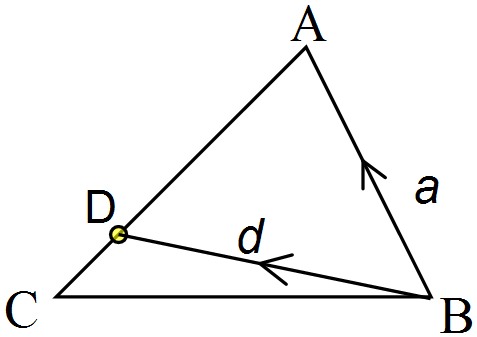
**Question 11 (6 marks)**

(a) A triangle  has vertices ,  and . Determine the vector ,

where  is the midpoint of side . (3 marks)

(b)  is a triangle with point  on side  such that . If and ,

show that . (3 marks)



**Question 12 (7 marks)**

(a) Vectors  have the same magnitude and vectors  are perpendicular, where  ,  and Determine the values of  and . (3 marks)

(b) Determine the scalar projection of a velocity of 12 m/s on a bearing of 65º onto a velocity of 20 m/s on a bearing of 280º, giving your answer to three significant figures. (2 marks)

(c) The work done, in joules, by a force of  Newtons in changing the displacement of an object by  metres is given by the scalar product of  and .

A force acting on a bearing of 160º does work of 1 200 joules. If the object moved a distance of 350 cm on a bearing of 135º, determine the magnitude of the force. (2 marks)

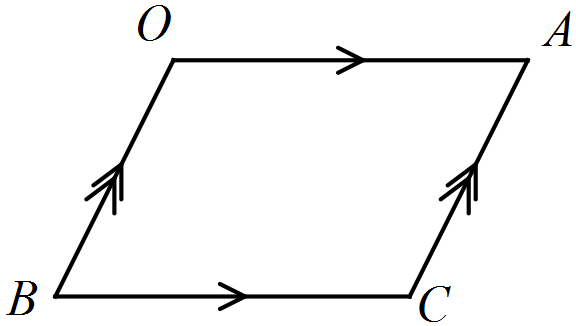
**Question 13 (8 marks)**

(a) A triangle has vertices at ,  and .

(i) Determine the vectors . (2 marks)

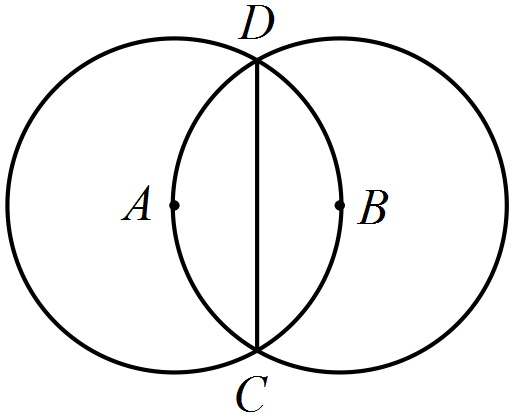
(ii) Use a vector method to prove that triangle  is right-angled. (2 marks)

(b) Use a vector method to prove that if the diagonals of a parallelogram are perpendicular to each other, then the parallelogram is a rhombus. (4 marks)

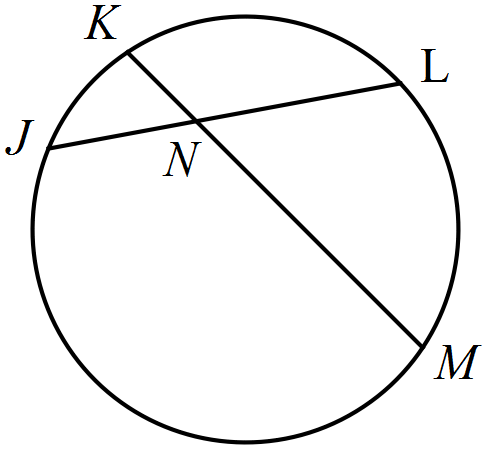


**Question 14 (9 marks)**

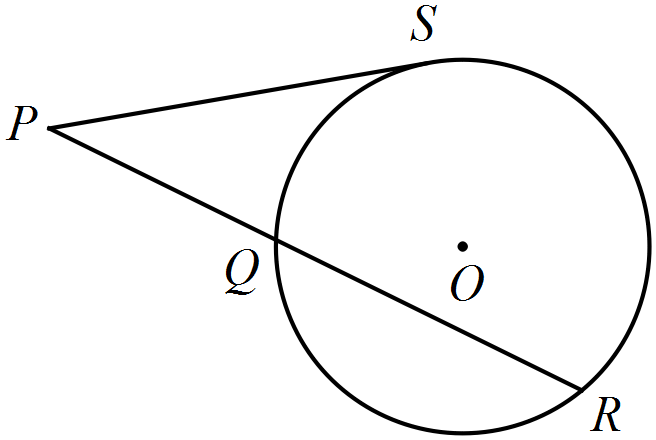
(a) Two circles of radius 12.6 cm, with centres  as shown below, have a common chord . Determine, with justification, the length . (3 marks)



(b) In the diagram below, . Determine, with justification, the exact length of . (3 marks)



(c) Determine the length, if that the length of chord  is 10.5 cm and the length of the tangent  is 9.5 cm. (3 marks)



**Question 15 (9 marks)**

(a) A small body A has position (12, -3) m relative to another small body B. If a third small body C has position (-5, 6) relative to A, determine the position of B relative to C.

(2 marks)

(b) To a cyclist moving with velocity (21, 5) km/h the wind appears to have velocity (9, 3) km/h. Determine the true speed of the wind. (2 marks)

(c) A small ship is travelling with a constant speed of 14 knots on a bearing of 025º and another, larger ship is travelling with a constant speed of 17 knots on a bearing of 310º.

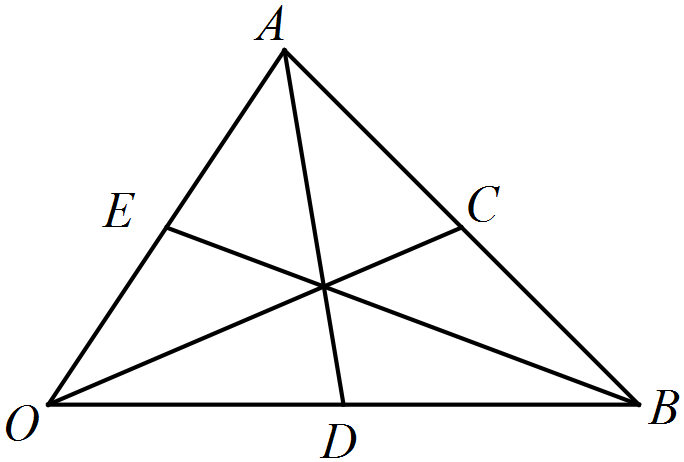
Determine the velocity of the large ship relative to the small ship. (5 marks)

**Question 16 (9 marks)**

The medians of triangle  are , as shown below.

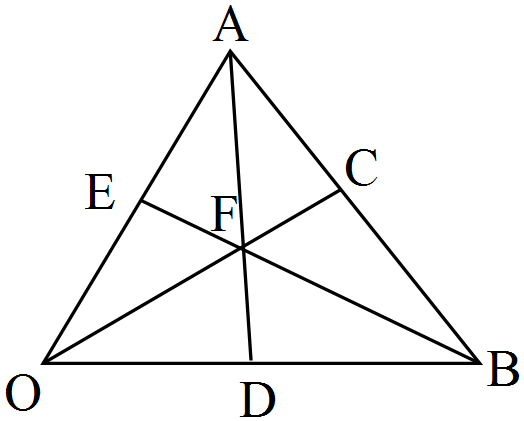
(A median joins a vertex to the midpoint of the opposite side of the triangle).

Let and



(a) Prove that . (4 marks)

(b) The centroid, , is the point of intersection of the medians.





Determine in terms of  ( and ). (5 marks)

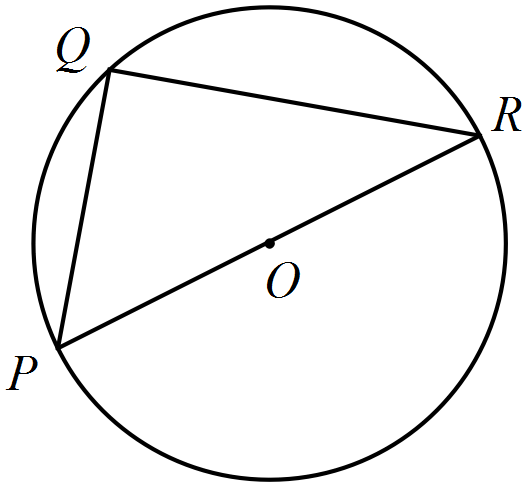
(*Hint: Let, , and first solve for  and *)

**Question 17 (8 marks)**

(a) The diagram shows a triangle with vertices  that lie on a circle with centre .

Chord  passes through . Prove, by contradiction, that angle  is acute.

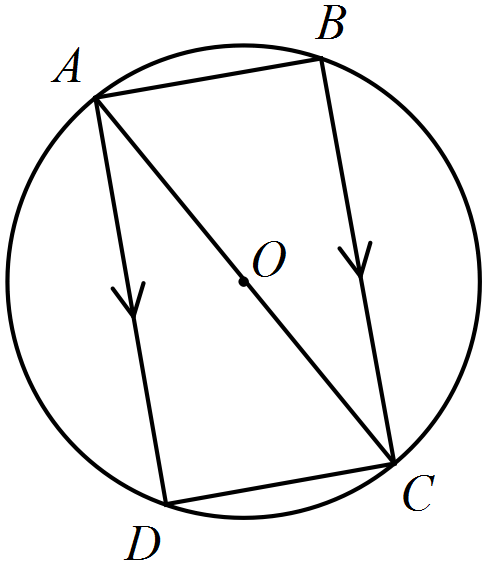
(4 marks)



(b) In the diagram below,  is the centre of the circle on which points *A, B, C* and *D* lie.

Chord *AC* passes through *O* and *BC* is parallel to *AD*

Prove that the quadrilateral *ABCD* is a rectangle. (4 marks)



**Question 18 (8 marks)**

(a) A small coach has 24 seats, arranged in six rows of four seats each, with two seats in each row on either side of the central aisle. A group of passengers consisting of ten males and nine females board the bus.

(i) Determine how many combinations of empty seats are possible once everyone has sat down. (1 mark)

(ii) How many fewer combinations are there if the females all sit on one side of the aisle and the males all sit on the other side? (3 marks)

(b) Determine the number of possible four letter permutations of the letters of the word

RELOAD. (1 mark)

(c) Determine the number of **different** 8 letter words possible from the letters of the word RELOADED. (2 marks)

(d) How many of the words in part (d) have the word “deed” within them? (1 mark)

Eg. “RODEEDAL”

**Question 19 (7 marks)**

A small boat has to travel across a river from  to , where  metres and metres. A uniform current of  m/s is flowing in the river and the boat can maintain a steady speed of 4 m/s.

(a) Determine, in the form , the velocity vector the small boat should set to travel directly from  to . (*Warning: Your calculator may take quite a while to solve the necessary equations, don’t panic!*)

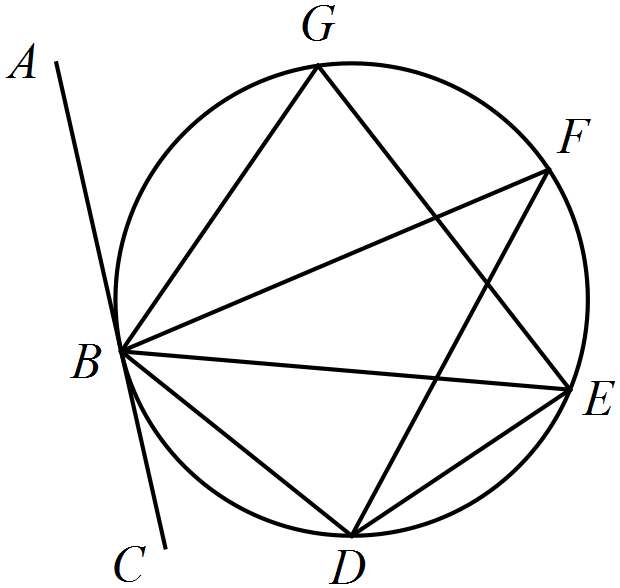
(5 marks)

(b) Calculate, to the nearest minute and second, how long the journey will take. (2 marks)

**Question 20 (7 marks)**

(a) In the diagram below,  is a tangent to the circle at . If ,  and , determine the size of angle .

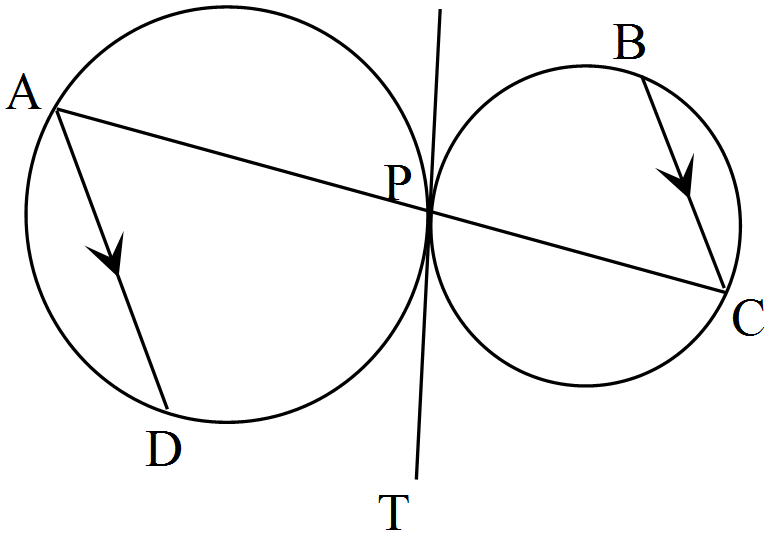
Clearly show your reasoning by filling in values on the diagram. (3 marks)



(b) In the diagram below, the line  passes through the point , where both circles touch each other. The line is parallel to line . *TP* is tangential to both circles at *P***.**

**Prove** that the points  are collinear.

(4 marks)



**Additional working space.**

**Question Number: \_\_\_\_\_\_\_\_\_**

**Additional working space.**

**Question Number: \_\_\_\_\_\_\_\_\_**